## Hitting a cricket ball

A 150 g cricket ball is bowled with a speed of $20 \mathrm{~ms}^{-1}$. The batsman hits it straight back to the bowler at $40 \mathrm{~ms}^{-1}$, and the impulsive force of bat on ball has the shape as shown.
(a) What is the maximum force the bat exerts on the ball?
(b) What is the average force the bat exerts on the ball?


Solution: From the impulse-momentum theorem,

$$
\begin{aligned}
J=\Delta p & =\text { area under force curve } \\
& =1 / 2 \times 0.6 \times 10^{-3} \times F_{\max } \\
& =3 \times 10^{-4} F_{\max }
\end{aligned}
$$

Now
$\Delta p=$ change in momentum
$=p_{\mathrm{f}}-p_{\mathrm{i}}$

$$
=m\left(v_{\mathrm{f}}-v_{\mathrm{i}}\right)
$$

$$
=0.15 \times(40+20)=9 \mathrm{~kg} \mathrm{~ms}^{-1}
$$

so equating this with the above expression for $J$, we get

$$
3 \times 10^{-4} F_{\max }=9 \mathrm{~kg} \mathrm{~ms}^{-1}
$$

so

$$
F_{\max }=9 / 3 \times 10^{-4}=30,000 \mathrm{~N}
$$

the maximum force that the bat exerts on the ball.

The average force $F_{\mathrm{av}}$ is

$$
F_{\max }=\Delta p / t=9 / 6 \times 10^{-4}=15,000 \mathrm{~N}
$$

